

Path Planning Techniques for Navigation of Mobile Robot: A survey

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Abstract: In this survey we have presented the detailed survey of path planning algorithms and techniques available so far. All the available methods and techniques are systematically understood and presented in the proper manner in order to make a research gap in the available techniques. The path planning algorithms are applied on static as well as in the dynamic environment. We also present the techniques based on these environments. The Approaches are classified into classical and reactive approaches. The classical approaches such as cell decomposition (CD), roadmap approach (RA), artificial potential field (APF); reactive approaches such as genetic algorithm (GA), fuzzy logic (FL), neural network (NN), firefly algorithm (FA), particle swarm optimization (PSO), ant colony optimization (ACO), bacterial foraging optimization (BFO), artificial bee colony (ABC), cuckoo search (CS), shuffled frog leaping algorithm (SFLA) and other miscellaneous algorithms (OMA) are considered for study. The navigational algorithms are applied on static as well as in the dynamic environment for analysis and it has been concluded that the reactive methods are more suitable for path planning and navigation of mobile robot.

I. Introduction:

Initially, the application of a mobile robot was limited to manufacturing industries only. But nowadays, it is commonly used in the fields of entertainment, medicine, mining, rescuing, education, military, space, agriculture and many more. While performing the task of navigation, the robot is equipped with many intelligent equipment's which are required to model the environment and localize its position, control the motion, detect obstacles, and avoid obstacles by using navigational techniques. Safe path planning (by detecting and avoiding the obstacles) from the initial position to the target position is the most important function of any navigational

technique. Therefore, the proper selection of the navigational technique is the most important step in the path planning of a robot when working in a simple and complex environment. At present, many techniques have been developed by various researchers in the field of mobile robot navigation and it is the most researched topic of today. Mobile robot navigation is classified into three categories: global navigation, local navigation and personal navigation. The capability to define the position of elements in the environment with respect to the reference axis, and to stir towards the pre-decided goal, is global navigation. Local navigation deals with the identification of the dynamic conditions of the environment and the establishment of positional relationships among various elements. To handle the various elements of the environment relative to each other, by considering their position, is personal navigation. The basic steps involved in the functioning of the robot [1] are presented in Fig. 1.

In this paper, the navigation strategy has been classified based on the prior information of the environment required for path planning. It is broadly classified as global navigation and local

navigation. In global navigation, the mobile robot must require the prior information of the environment, obstacle position and goal position whereas in local navigation the mobile robot does not require the prior information of the environment. Global navigation strategy deals with a completely known environment. Local navigation strategy deals with the unknown and partially known environment. The path planning algorithm for a known environment is based on a classical approach such as CD, RA, and APF. These algorithms are traditional and have limited intelligence. Local navigational approaches are known as reactive approaches as they are more intelligent and able to control and execute a plan autonomously.

II. Navigational techniques used for mobile robot navigation

2.1 Traditional approaches:

Initially, classical approaches were very popular for solving robot navigational problems because in those days artificially intelligent techniques had not been developed. By using classical approaches for performing a task, it is observed that either a result would be obtained, or it would be confirmed that a result does not exist. The major drawback of this approach is high computational cost and failure to respond to the uncertainty present in the environment; therefore, it is less preferred for real-time implementation. CD, RA, and APF are some of the classical approaches which are reviewed here.

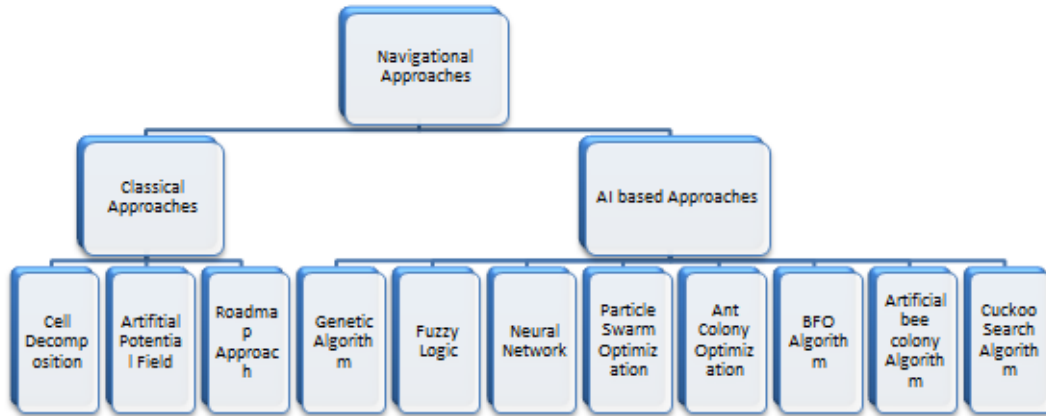


Figure-1: Mobile robot Navigational Approaches

2.1.1 Cell decomposition (CD) approach

This approach divides the region into non-overlapping grids (cells) and uses connectivity graphs for traversing from one cell to another to achieve the goal. During traversing, pure cells (cells without obstacles) are considered to achieve path planning from the initial position to the target position. Corrupted cells (cells containing obstacles) present in the path are further divided into two new cells to get a pure cell and this pure cell gets added to the sequence while determining the optimal path from the initial position to the target position. In the CD approach, the initial position and target position are represented by the start and end cells. The CD approach is classified as adaptive, approximate and exact.

2.1.2. Roadmap approach (RA)

The RA is also known as the highway approach. It is the way to get from one place to another and the connection among the free spaces is represented by a set of one-dimensional curves [22]. When the roadmap is built, then it is utilized as an arrangement of homogeneous ways where the planner will seek to discover the ideal arrangement. Here, nodes play an important role in getting the desired path for the robot. The RA is used to find the shortest path from the robot's initial position to its target position; Voronoi and visibility graphs are used to develop the roadmap. The visibility graph method connects the initial and the goal position with nodes from the map. This method is also used for an environment with polygonal obstacles in which the vertices of the polygon are represented by the nodes and edges as a connector between the nodes [24]. The Voronoi diagram is another roadmap algorithm used for the path planning of the robot. This method divides the region into sub-regions where all the edges of the figure are constructed using equidistant points from the adjacent two points on the obstacle's boundaries. The application of the Voronoi diagram in the field of mobile robot navigation around obstacles is presented.

2.1.3 Artificial potential field (APF) approach

In APF approach, the goal and obstacles act like charged surfaces and the total potential creates the imaginary force on the robot. This imaginary force attracts the robot towards the goal and keeps it away from an obstacle. Here, the robot follows the negative gradient to avoid the obstacle and reach the target point. Application of this method for mobile robot navigation is presented by Garibotto et al. [39]. A new obstacle avoidance strategy in an unknown environment is discussed by Kim et al. [40] by using APF. They used a harmonic function to avoid a local minimum problem. Borenstein et al. [41] have also presented a solution to

the problem of the local minima conditions. In this research, they have considered the dynamic properties of robot navigation.

2.2 Artificial Intelligence based Approaches: AI based approaches are more popular as they have the ability to deal an uncertain environment quickly with less computational effort.

2.2.1 Genetic algorithm (GA)

This is a popular search-based optimization tool which follows the principle of genetics and natural selection. Its application to the field of computer science was presented first by Holland [56] in 1975. Nowadays, it has wide application in all areas of science and technology including robot navigation. In this approach, the population (different individuals characterized by genes) must be allotted for the given problem and every member of the population is assigned with a fitness value depending upon the objective function. These individuals are selected as per their fitness value and allowed to pass their genes to a new generation by crossover. The mutation maintains the diversity in population and prevents premature convergence. Finally, the algorithm is terminated if the population has converged. Although the GA is randomized in nature to some extent, its performance is better as they can exploit historical information as well when compared to a random local search.

2.2.2 Fuzzy logic (FL)

The concept of FL was given first by Zadeh [77] in 1965 and was later on used in all the fields of research and development. It is used in situations where there is a high degree of uncertainty, complexity, and nonlinearity. Pattern recognition, automatic control, decision making, data classification are a few of them. The hypothesis of the FL framework is encouraged by the noteworthy human ability to process perception-based information. It uses the human-supplied rules (If-Then) and converts these rules to their mathematical equivalents. This streamlines the job of the system designer and computer for getting more correct information about the way systems perform in the real world and hence it is used for path planning of a mobile robot.

2.2.3 Neural network (NN)

Artificial NN is an intelligent system which consists of many simple and highly interconnected processing elements. These elements transfer the information by their capability of dynamic state response to external inputs. The NN is basically shown by well-organized layers of interconnected nodes. The nodes consist of an activation function. The input layer of the NN mechanism recognizes the patterns. These patterns then communicate to hidden layers for actual processing via a system of weighted connections. The hidden layers connect with the output layer to give the required answer. NN characteristics such as generalization ability, massive parallelism, distributed representation, learning ability and fault tolerance make it useful in the field of mobile robot navigation.

2.2.4 Particle swarm optimization (PSO)

This is a nature-based metaheuristic algorithm which adopts the social behavior of creatures such as fish schools and bird flocks. It is developed by Eberhart and Kennedy [117] in 1995 and it is a rapidly growing optimization tool for solving the various problems of engineering and science. The PSO mimics the behavior of the social animal but does not require any leader within the group to reach the target. When the flock of birds goes to find food, they do not require any leaders; they go with one of the members who is at the nearest position to the food (Fig. 15). In this way, the flock of birds reaches their required solution by proper communication with the members of the population. The PSO algorithm consists of a group of particles where each particle represents a potential solution. Nowadays, PSO is widely used in the field of mobile robot navigation.

2.2.5 Ant colony optimization (ACO)

This is a swarm intelligence algorithm which is a population-based approach used to solve the combinatorial optimization problem. The ACO algorithm originated from the behavior of ants and its ability to find the shortest path from their nest to a food source. The ACO algorithm is already applied to various fields of science and engineering such as job-shop scheduling, vehicle routing, quadratic assignment problem, travelling salesman problems, graph coloring and many more. Nowadays, the ACO is used to handle the mobile robot navigation problem for obstacle avoidance and effective path planning.

2.2.6 Bacterial foraging optimization (BFO) algorithm

Passino [123] in 2002 presented the new nature-inspired optimization algorithm which is originated from the behavior of an *E. coli* and *M. Xanthus* bacteria. These bacteria search for nutrients by making the best use of energy achieved per unit time. The BFO algorithm is featured by chemotaxis that perceives chemical gradients by which bacteria communicate specific signals with each other. It has four basic principles such as chemotaxis, swarming, reproduction and elimination, and dispersal. The behavior of the bacteria [124] for searching the nutrient region is presented as below and explained in Fig. 19.

- _ Bacteria always travel in search of more nutrient regions on the map. Bacteria with sufficient food have a longer life and split into two equal parts whereas bacteria in the lesser nutrient region will disperse and die.
- _ Bacteria present in the more nutrient region are attracted together by chemical phenomenon and those who are in the lesser nutrient region give a warning signal to other bacteria using a specific signal.
- _ Bacteria get a highly nutrient region on the map.
- _ Bacteria are dispersed again in the map for a new region of nutrients.

2.2.7 Artificial bee colony (ABC) algorithm

The ABC algorithm is a swarm-based intelligent approach inspired by the activities of honey bees in search of food and is proposed by Kharaboga [125]. The ABC algorithm is a population-based strategy consisting of a population of inherent solutions (food source for bees). It is relatively simple in use, fast in processing and is a population-based stochastic search approach in the field of swarm algorithms.

2.2.8 Cuckoo search (CS) algorithm

The CS algorithm is a metaheuristic algorithm presented by Yang and Deb [136] in 2009. The algorithm is based on the lazy behavior of some cuckoos for laying their own eggs in the nests of other host birds. According to Yang, the algorithm follows three basic rules for an optimization problem as follows.

- _ Each cuckoo lays one egg at a time in a randomly chosen nest.
- _ The best nests with high-quality eggs will be carried over to the next generation.
- _ The number of available host nests is fixed, and the egg laid by a cuckoo may be discovered by the host bird with a probability $p_a(0, 1)$.

In this case, the host bird can either get rid of the egg or simply abandon the nest and build a completely new nest. The CS algorithm is an improved method because it increases the convergence rate and efficiency hence it is widely accepted in various engineering optimization problems; mobile robot navigation is one area where performance and computational time is to be optimized.

III. Conclusion:

After systematically presenting the survey on mobile robot navigation methodologies, all the methods are classified into two categories. They are Traditional and Artificial Intelligence based approaches. The key points of the study are as follows.

- _ Artificial based approaches perform better than classical approaches because they have a higher capability to handle uncertainty present in the environment.
- _ Artificial based approaches are most preferably used for real-time navigation problems.
- _ Very few research papers are published based on a dynamic environment compared with a static environment.
- _ In a dynamic environment, there are many fewer papers on navigation of a robot for a moving goal problem compared with a moving obstacle problem.
- _ To date, most papers demonstrate only a simulation analysis; papers on the real-time application are much fewer.
- _ Papers on the navigation of multiple mobile robot systems are few compared with the single mobile robot system.
- _ There are many fewer papers on hybrid algorithms compared with those on standalone algorithms.
- _ There is great scope in applying newly developed algorithms such as SFLA, CS, IWO, BA, HS, DE, BFO, ABC and FA for navigation in an unknown complex environment in the presence of maximum uncertainty and these can be used to develop new kinds of hybrid approaches.
- _ The performance of classical approaches can be improved by hybridizing with Artificial based approaches.

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